

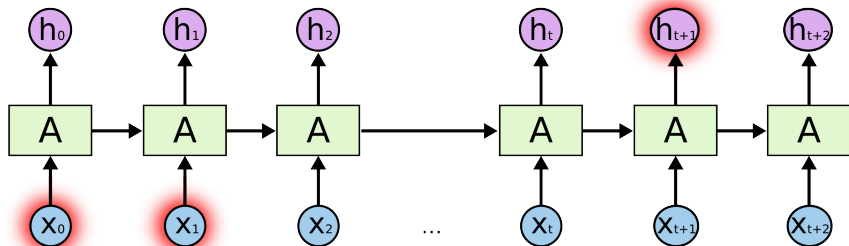
# Deep Learning

Vazgen Mikayelyan

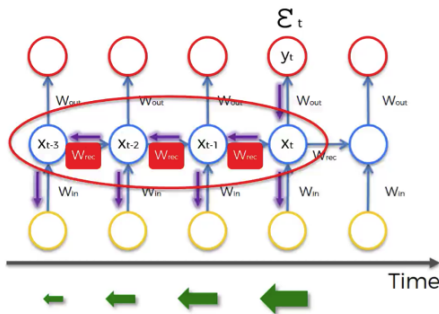
December 1, 2020



# Problem of Long Term Dependencies



## The Vanishing Gradient Problem



$$\frac{\partial \mathcal{E}}{\partial \theta} = \sum_{1 \leq t \leq T} \frac{\partial \mathcal{E}_t}{\partial \theta} \quad (3)$$

$$\frac{\partial \mathcal{E}_t}{\partial \theta} = \sum_{1 \leq k \leq t} \left( \frac{\partial \mathcal{E}_t}{\partial \mathbf{x}_t} \frac{\partial \mathbf{x}_t}{\partial \mathbf{x}_k} \frac{\partial^+ \mathbf{x}_k}{\partial \theta} \right) \quad (4)$$

$$\frac{\partial \mathbf{x}_t}{\partial \mathbf{x}_k} = \prod_{t \geq i > k} \frac{\partial \mathbf{x}_i}{\partial \mathbf{x}_{i-1}} = \prod_{t \geq i > k} \mathbf{W}_{rec}^T \text{diag}(\sigma'(\mathbf{x}_{i-1})) \quad (5)$$

$W_{rec} \sim \text{small} \rightarrow \text{Vanishing}$   
 $W_{rec} \sim \text{large} \rightarrow \text{Exploding}$

Formula Source: Razvan Pascanu et al. (2013)

- 1 GRU and LSTM
- 2 Bidirectional and Deep RNNs
- 3 Attention Models

# Simple RNN



Neural Network  
Layer



Pointwise  
Operation



Vector  
Transfer

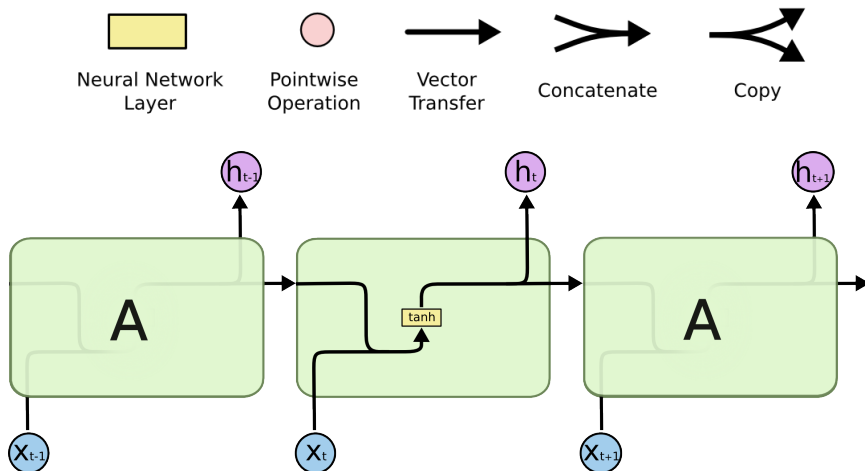


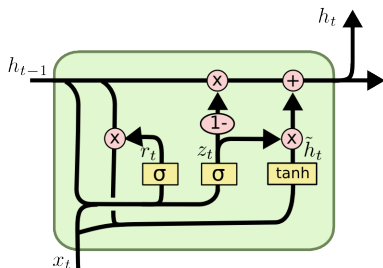
Concatenate



Copy

# Simple RNN



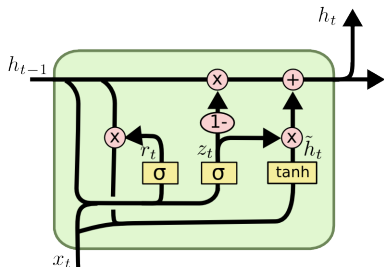


$$z_t = \sigma(W_z \cdot [h_{t-1}, x_t])$$

$$r_t = \sigma(W_r \cdot [h_{t-1}, x_t])$$

$$\tilde{h}_t = \tanh(W \cdot [r_t * h_{t-1}, x_t])$$

$$h_t = (1 - z_t) * h_{t-1} + z_t * \tilde{h}_t$$



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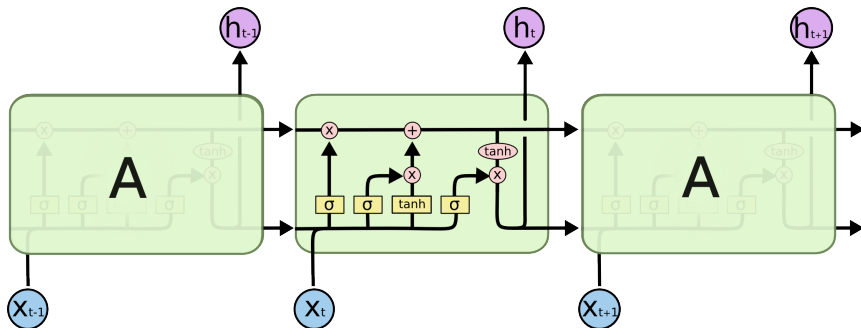
Concatenate



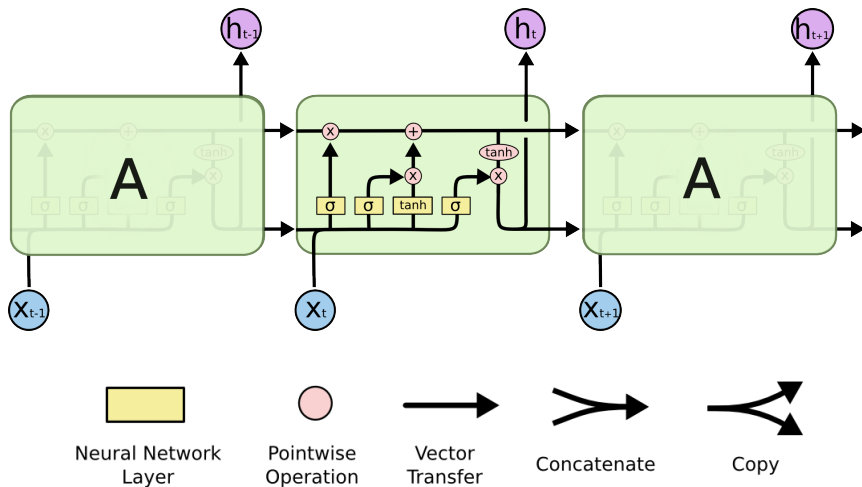
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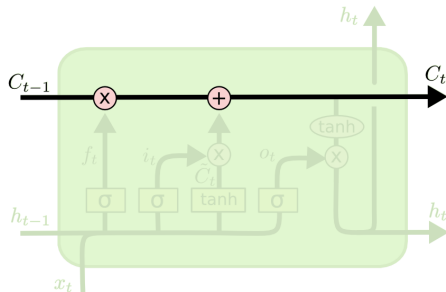
# LSTM



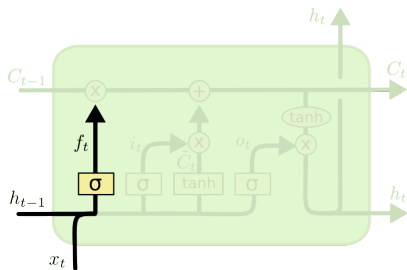
# LSTM



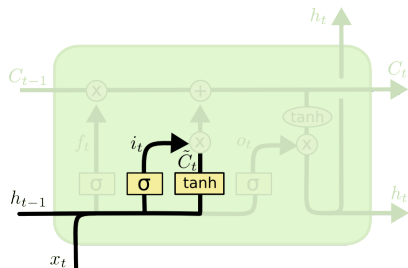
# Additional state



# LSTM



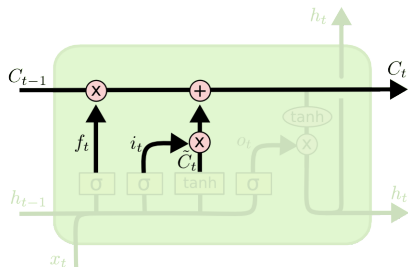
$$f_t = \sigma (W_f \cdot [h_{t-1}, x_t] + b_f)$$



$$i_t = \sigma(W_i \cdot [h_{t-1}, x_t] + b_i)$$

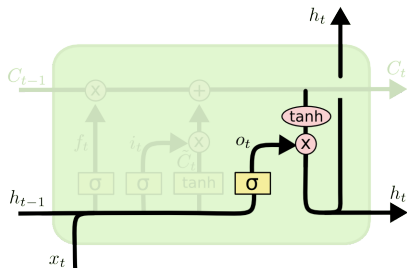
$$\tilde{C}_t = \tanh(W_C \cdot [h_{t-1}, x_t] + b_C)$$

# LSTM



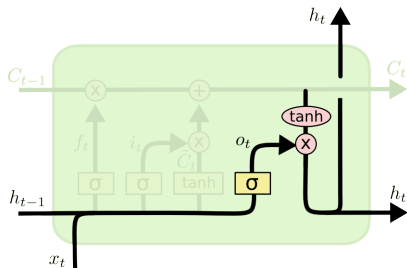
$$C_t = f_t * C_{t-1} + i_t * \tilde{C}_t$$

# LSTM



$$o_t = \sigma(W_o [h_{t-1}, x_t] + b_o)$$

$$h_t = o_t * \tanh(C_t)$$



$$o_t = \sigma(W_o [h_{t-1}, x_t] + b_o)$$

$$h_t = o_t * \tanh(C_t)$$

Why to use tanh?



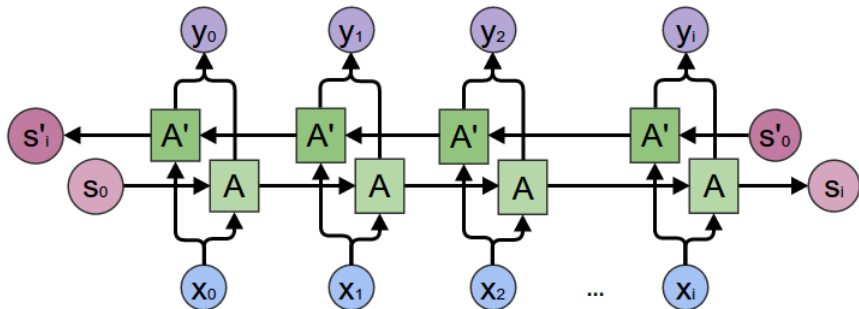
# Outline

1 GRU and LSTM

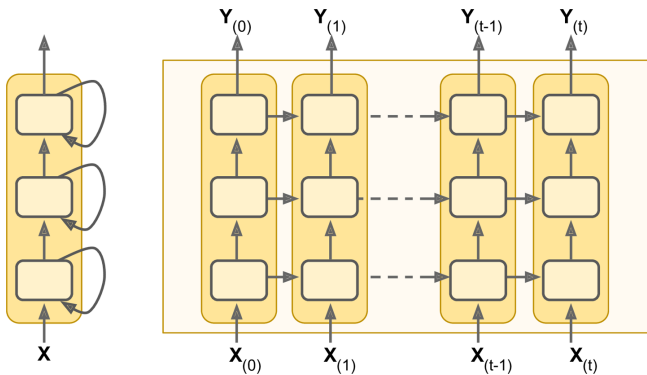
2 Bidirectional and Deep RNNs

3 Attention Models

# BiRNN



# Deep RNNs



# Outline

1 GRU and LSTM

2 Bidirectional and Deep RNNs

3 Attention Models

- Encode each word in the sentence into a vector using RNNs.

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- When decoding, perform a convex combination of these vectors, weighted by “attention weights”.

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- When decoding, perform a convex combination of these vectors, weighted by “attention weights”.
- Use this combination in picking the next word.

# Attention Model

